## Majority Rule in Harmonic Serialism

## Introduction

Optimizing over constraints defined in terms of precedence relations produces pathologies - Precedence relations define subsequences, objects without locality or adjacency

- Case study: requiring subsequences to agree yields Majority Rule in Harmonic Serialism - Other cases: Midpoint pathology (Eisner, 1997, 2000) \& Bubble Sort (Lamont, 2018)

Majority Rule largest class in the input controls agreement (Lombardi, 1999; Baković, 2000) *technically plurality rule


Running example: [s] cannot co-occur with [J] (*s. . .f, *. . . s); inputs with both /s/ and /f/ $\Rightarrow$...surface only with [s] if underlyingly there are more /s/ than $/ \mathrm{j} /(m>n)$
$\Rightarrow$...surface only with [J] if underlyingly there are more $/ \mathrm{s} /$ than $/ \mathrm{s} /(m<n)$ Majority Rule in parallel Optimality Theory
Necessary ranking: AGREE constraint(s) >> IDENT constraint
$\Rightarrow$ Constraints preferring one class must be ranked low enough as to be inactive

- In parallel OT, Majority Rule optimizes faithfulness constraints
$\Rightarrow$ Candidates that satisfy Agree compete in terms of Ident
$\Rightarrow$ Optimal candidate makes fewest changes, minimally violating IDENT
All else equal, predicted whenever multiple unfaithful candidates satisfy output constraints

| /f ...f...f...s...s/ | $\operatorname{Corr}$ (SIB) | CC-Ident(Ant)[Global ~ Local] | Ident(ant) |
| :---: | :---: | :---: | :---: |
| a. $\int \ldots \int \ldots \int \ldots s \ldots s$ | W 10 |  | L |
| b. $\square$ |  | W $6 \sim$ W 1 | L |
| $\rightarrow \mathrm{c} . \int_{i} \ldots \int_{i} \ldots \int_{i} \ldots$ (i) $\ldots$ (Ji |  |  | 2 |
| d. $s_{i} \ldots$. $s_{i} \ldots \ldots s_{i} \ldots s_{i} \ldots s_{i}$ |  |  | W 3 |

## Why investigate subsequences?

Phonotactic generalizations co
TSL bans marked substrings
$\left.\begin{array}{l}\text { TSL bans marked substrings on a tier } \\ \text { SP bans marked subsequences }\end{array}\right\}$ Long-distance phenomena
Provide well-defined hypothesis space for investigating classes of output constraints

| +1 | REG | $<$ |
| :---: | :---: | :---: |
|  |  | NC |
| LTT TSL |  |  |
| LT PT |  |  |
|  |  |  |
| SL |  |  |

FIN

## Majority Rule in Harmonic Serialism

- In HS, candidates only differ from the input via at most one unfaithful operation - Unfaithful candidates can violate a given faithfulness constraint at most once
$\Rightarrow$ No arbitrarily large differences in violations of any faithfulness constraint
$\Rightarrow$ Mechanism that produces Majority Rule in parallel OT does not exist in HS
- Majority Rule is unexpected in HS, but it optimizes globally evaluated CC-Ident

Global and local evaluation in Agreement by Correspondence

- $\operatorname{Corr(SIB):~Assign~one~violation~for~each~pair~of~sibilants~that~do~not~correspond~}$
- CC-Ident(Ant): Assign violations for pairs of correspondents disagreeing in [anterior] Global evaluation: every pair of Local evaluation: only chain-adjacent $\underset{* * *}{\text { correspondents are possible loci pairs of correspondents are possible loci }}$ $\underbrace{\int_{i \ldots S_{i} \ldots s_{i} \ldots s_{i} \ldots s_{i}}^{* *}}_{* * *} \quad(\approx \mathbf{S P})$ $\int_{i} \ldots \int_{i} \ldots \int_{i} \ldots s_{i} \ldots s_{i} \quad(\approx$ TSL $)$
(Bennett, 2013, 2015; Hansson, 2001, 2007, 2010, 2014; Rose \& Walker, 2004; Walker, 2000, 2015)
Globally evaluated CC-Ident produces Majority Rule in HS
- Candidates with corresponding sibilants violate CC-IDENT(ANT) to various degrees - Targeting member of minority class removes more loci than are added - always optimal

| Step 1: /f ... . . . . . . . ...s/ | Corr(sib) | CC-Ident(ant)[Global] | Ident(ant) |
| :---: | :---: | :---: | :---: |
| a. $\int \ldots \int \ldots \int \ldots s \ldots s$ | W 10 |  | L |
| b. $\square$ $\underbrace{{ }_{i} \ldots{\sqrt[S]{i} \ldots s_{i} \ldots s_{i} \ldots s_{i}^{*}}_{*}^{*}}_{i \ldots *}$ |  | W 6 | L |
|  |  | 4 | 1 |
| d. $\square$ $\frac{i_{k * *}{\sqrt{i} \ldots s_{i} \ldots s_{i} \ldots s_{i}}^{* * *}}{}$ |  | W 6 | 1 |
| Step 2: $\int \ldots \int \ldots \int \ldots \int \ldots s$ | Corr(sib) | CC-Ident(ant)[Global] | $\operatorname{ldent(Ant)~}$ |
| a. $\int \ldots \int \ldots \int \ldots \int \ldots s$ | W 10 |  | L |
| b. $\sqrt{\int_{i} \ldots \sqrt{i}_{i} \ldots{\sqrt{i} \ldots \int_{i} \ldots s_{i}}_{*}^{*}}$ |  | W 4 | L |
| $\rightarrow$ c. $\int_{i} \ldots \int_{i} \ldots \int_{i} \ldots \int_{i} \ldots$. d $^{\text {d }}$ |  |  | 1 |
| d. |  | W 6 | 1 |

Locally evaluated CC-Ident cannot produce Majority Rule (or iterative harmony) in HS

- With local evaluation, each change creates as many new loci as are removed
- Iterative harmony is harmonically bounded (Wilson, 2003; Pater et al., 2007)

| Step 1: /f ...f...f..s...s/ | Corr(sib) | CC-Ident(ant)[Local] | Ident(ant) |
| :---: | :---: | :---: | :---: |
| a. $\int \ldots \int \ldots \int \ldots s \ldots s$ | W 10 |  |  |
| $\rightarrow \text { b. } \int_{i} \ldots s_{i} \ldots \int_{i} \ldots s_{i} \ldots s_{i}$ |  | 1 |  |
| c. $\int_{i} \ldots \int_{i} \ldots \int_{i} \ldots \int_{i j} \ldots s_{i}$ |  | 1 | W 1 |
| d. $\int$ |  | 1 | W 1 |

## Directional Constraint Evaluation

- Globally-defined constraints motivate iterative spreading in HS, but also overgenerate Locally-defined constraints undergenerate, but represent intuitive generalizations
$\Rightarrow$ Spreading as myopic (Wilson, 2003, 2006)
$\Rightarrow$ Local exceptions in vowel harmony (Finley, 2010)
$\Rightarrow$ Blocking in harmony and dissimilation (McMullin \& Hansson, 2015; McMullin, 2016) Iterative harmony with directional output constraints

$\Rightarrow$ Global constraints cannot pool large numbers of loci $\rightarrow$ no Majority Rule
$\Rightarrow$ Local constraints can differentiate between loci $\rightarrow$ yes iterative spreading
Output constraints are specified for directionality: $R \rightarrow L$ or $L \rightarrow R$
$\Rightarrow R \rightarrow L$ evaluation disprefers loci later in candidates - further to the right is worse
$\Rightarrow$ Relative position of loci defined over lexicographical order of segment indices

| Step 1: / $\ldots \ldots$. $\ldots$ S $\ldots$. ...s/ | Agree(sib, ant $)_{R \rightarrow L}$ |  |  | Ident(ant) |
| :---: | :---: | :---: | :---: | :---: |
| $\rightarrow$ a. $\int \ldots f \ldots$..s...s...s | $\sigma_{2} \sigma_{3}$ |  |  | 1 |
| b. $\int \ldots$.....f...s...s | W | $\sigma_{3} \sigma_{4}$ |  | L |
| $\text { c. } \frac{\ldots}{} \ldots \ldots \rho \ldots$ | W |  | $\sigma_{4} \sigma_{5}$ | 1 |

Directional HS derivations resemble linear rule application (Johnson, 1972)
$\Rightarrow$ Rightmost target repaired at each step, application proceeds strictly leftwards
$\Rightarrow$ Each step is regular (Eisner, 2000); derivations seem to be as well (proof forthcoming)

## lustration: Ineseño Chumash directional harmony

Regressive sibilant harmony
Dissimilation between morphemes
Dissimilation blocks \& feeds harmony
(Applegate, 1972; McCarthy, 2007)
s-kamisa-ts/ $\rightarrow$
[kamiJaat5] 'he wears a shirt'
strikkun/ $\rightarrow$ [stumukun] 'mistletoe' s-tepu?/ $\rightarrow$ [Jtepu?] 'he gambles' s-ti-yep-us/ $\rightarrow$ [Jtiyepus] 'he tells him s-is-tit?/ $\rightarrow[\mathrm{jj}$ 'ti? $] \quad$ he finds it Step :/s-in

| Step 1: /s-ij-lu-sisin/ | IdentTail | OCP | CrispEdge | Agree(sib,ant $)_{R \rightarrow L}$ |  |  | Ident |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a. sijlusisin |  |  |  | W $\sigma_{1} \sigma_{2}$ | $\sigma_{2} \sigma_{3}$ |  | L |
| b. sijlusij in | W1 |  |  | W $\sigma_{1} \sigma_{2}$ | $\sigma_{2} \sigma_{3}$ | $\sigma_{3} \sigma_{4}$ | 1 |
| c. sislusisin |  | W1 |  | L |  |  | 1 |
| d. sislusisin |  |  | W1 | L |  |  | 1 |
| e. sijlufisin |  |  |  | W $\sigma_{1} \sigma_{2}$ |  | $\sigma_{3} \sigma_{4}$ | 1 |
| $\rightarrow$ f. fijlusisin |  |  |  |  | $\sigma_{2} \sigma_{3}$ |  | 1 |

- Inconsistent with harmony as autosegmental spreading (McCarthy, 2007), ruling out a possible tier-based Share constraint (McCarthy, 2010)


## Conclusion and Future Directions

- Output constraints over subsequences are too powerful; local constraints are underpowered - Directional evaluation maintains local generalizations and the right amount of power - Directional-dominant harmony systems (Cook, 1979; Mahanta, 2007; Ribeiro, 2002, 2012) - Possible replacement of Align-also over subsequences (McCarthy, 2003; Hyde, 2012, 2016)
- Are subsequence constraints ever empirically necessary?
- Theory-internal solution to divergent ties (Pruitt, 2009)

Prove whether derivations are computationally regula

